

Modeling Software Systems

WALTER DOSCH

Institute of Software Technology and Programming Languages
University of Lübeck
Lübeck, Germany

<http://www.isp.uni-luebeck.de>



WALTER DOSCH
Institute of Software Technology and Programming Languages
University of Lübeck, Germany

Academica X
Tartu, Estonia
September 26, 2006

Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

7. Model Transformation

[8. Programming Language Models]

9. Classification of System Models

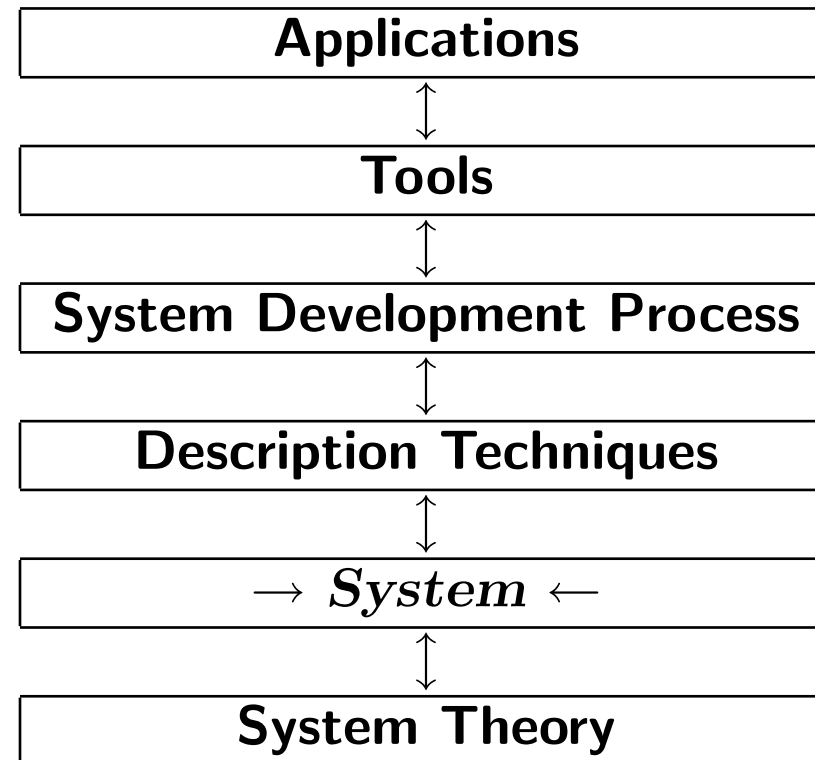


1.1 Current Trends in Information Technology

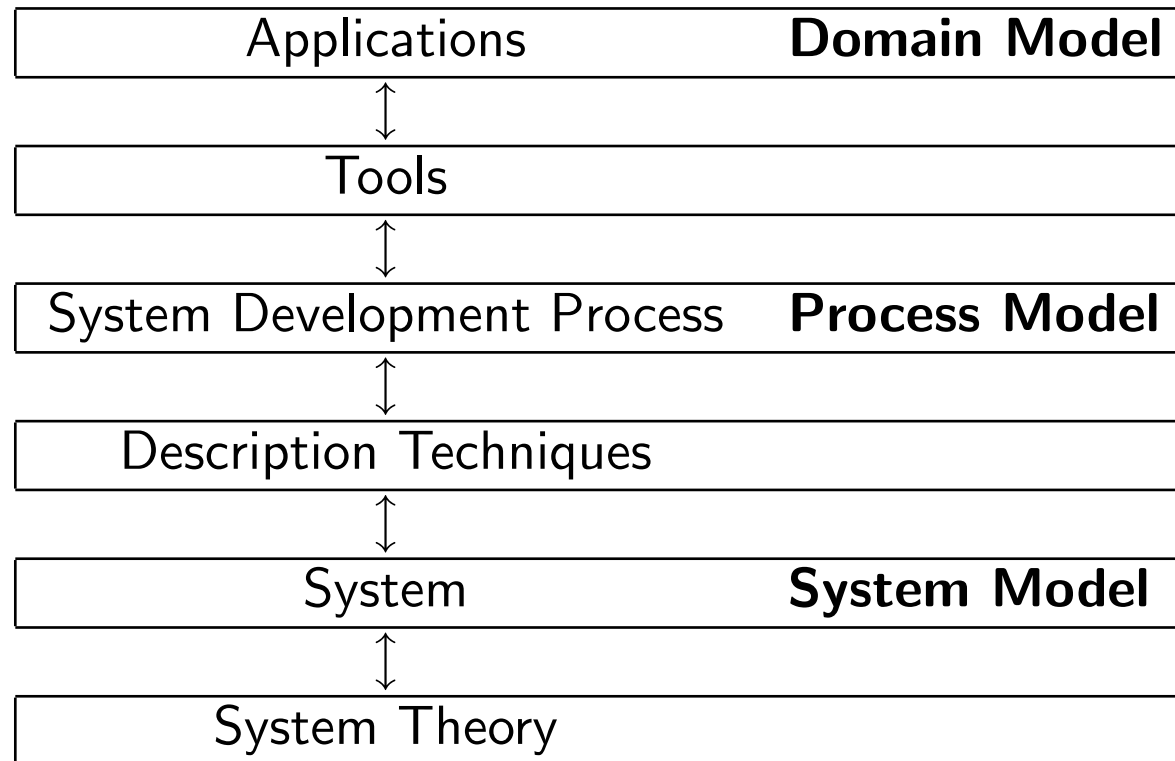
- **Hardware performance increases:**
computing power — storage capacity — transmission rate
- Growing **functionality** and **complexity**
- Worldwide **connectivity** — *networked infrastructures*
- **Interoperability** and **dependability** — *safety and security*
- **Industrial standards** — *scientific progress*
- **Reusability** of *products, artefacts* and *processes*
- Software is **embedded** into **engineering products**.
- Emerging **discipline of software engineering**
specification — modeling — design — implementation — (re)use
- **Modeling software systems**
structure — properties — behaviour . . . ↔ abstraction



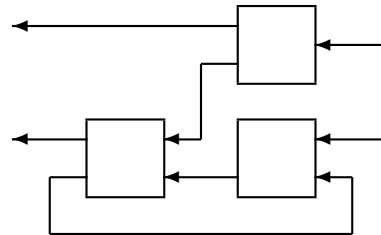
1.2 Layers of Software Technology



1.3 Modeling in Software Technology



1.4 System Model: Networks of Components



- **Complex systems** are networks of *software/hardware components*.
- Systems are **hierarchically composed** of (elementary) components.
- Components **cooperate** and **interact** by *exchanging information*.
- Components **communicate** sending *messages on directed channels*.
- **Specifications** define the *interface* and the *input/output behaviour*.



1.5 Application Areas

Service-oriented Classification

- Processing units
- Memory components
- Transmission components
- Synchronization and control components

Application-oriented Classification

- Process control
- Man-machine interaction
- Telecommunication
- Distributed computation



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

7. Model Transformation

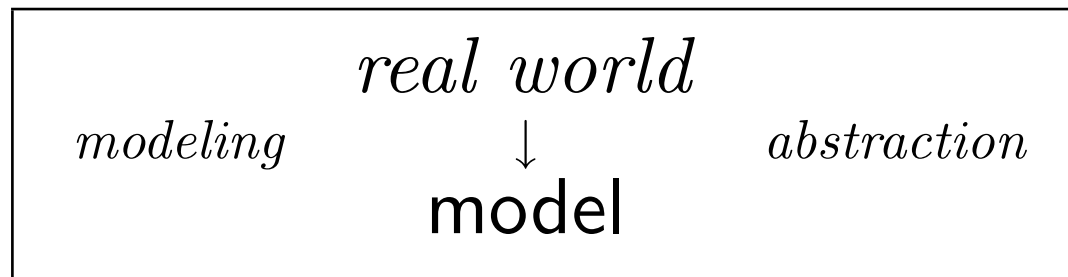
8. Programming Language Models

9. Classification of System Models



2.1 Modeling — Overview

A **model** [lat. *modulus*] is an **artefact** which describes certain **aspects** of a **part** of the **world** by its **similarity** in **structure**, **function**, **behaviour** or **use**.



- Four Areas*
- **Pragmatics** diagrams, plans, terminology, aspects
 - **Formalism** preciseness, adequacy, expressiveness
 - **Methods** modeling, validation, transformation
 - **Tools** analysis, checking, visualisation, generation



2.2 Modeling — Areas

foundations

ontologies

model integration

generative models

model validation

standardization

model-driven architectures

modeling nonfunctional requirements

model-based refactoring

enterprise application model

models for distributed control

model animation

modeling techniques

logic-based models

model transformation

pattern for modeling

model verification

model consistency

model engineering

aspect-oriented modeling

model-based reengineering

business process model

models for safety and security

modeling tools

model simulation

model quality



2.3 Modeling Components — *Views*

Data Structure	Communication-Based Description	State-Based Description	Trace-Based Description
<i>Data Model</i>	<i>Interaction Model</i>	<i>State Model</i>	<i>Process Model</i>

UML

- *Class diagrams* ↔ data structure
- *State machines* ↔ state-based description
- *Sequence diagrams* ← communication-based description

Description Techniques

- Equational logic ↔ functional style
- Predicate logic ↔ relational style
- State transition systems ↔ tabular and graphic style



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

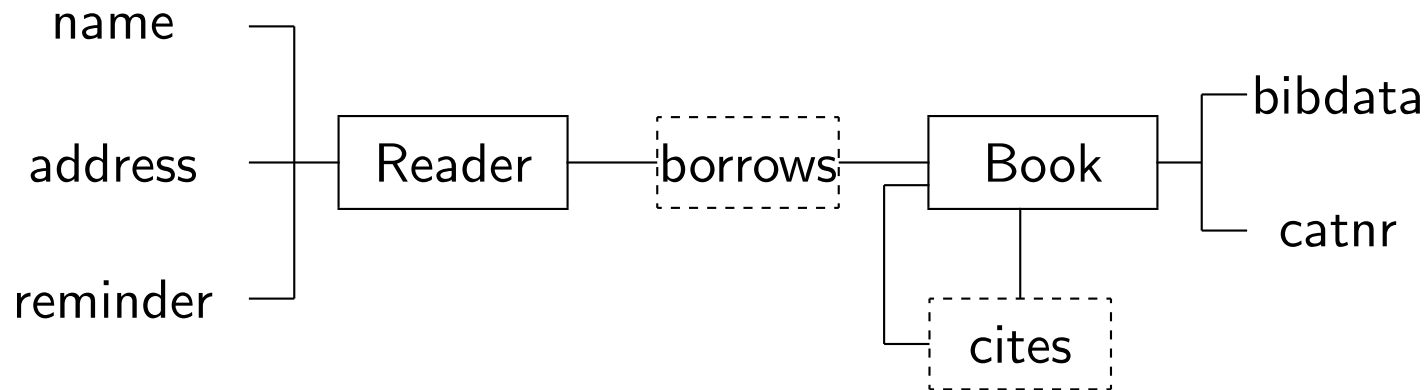
7. Model Transformation

8. Programming Language Models

9. Classification of System Models



3.1 Data Model — Entity Relationship Modeling



- **Sets** Reader, Book
- **Attributes**

name	Reader	→	String
address:	Reader	→	String
reminder:	Reader	→	Bool
...			
- **Relations**

borrows	\subseteq	Reader × Book
cites	\subseteq	Book × Book



3.2 Algebraic Specification — *Stacks*

An **algebraic specification** defines a *data structure* by the **properties** of its basic **operations** in a *representation independent way*.

STACK

$$\text{empty} : \rightarrow \text{stack}$$
$$\text{prefix} : \text{data} \star \text{stack} \rightarrow \text{stack}$$
$$\text{first} : \text{stack} \rightarrow \text{data}$$
$$\text{rest} : \text{stack} \rightarrow \text{stack}$$

$$\text{first}(\text{empty}) = \text{undefined}$$
$$\text{first}(\text{prefix}(d, s)) = d$$
$$\text{rest}(\text{empty}) = \text{undefined}$$
$$\text{rest}(\text{prefix}(d, s)) = s$$

abstract data type =

signature
<i>interface</i>

 +

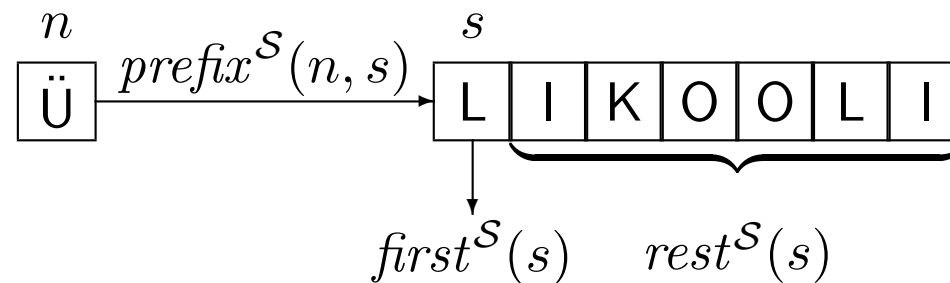
axioms
<i>behaviour</i>



3.3 Functional Data Model — *Stacks based on Sequences*

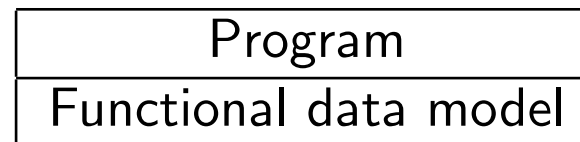
A **functional data model** defines the **carrier sets**, **functions** and **relations** of a data structure.

Model \mathcal{S}



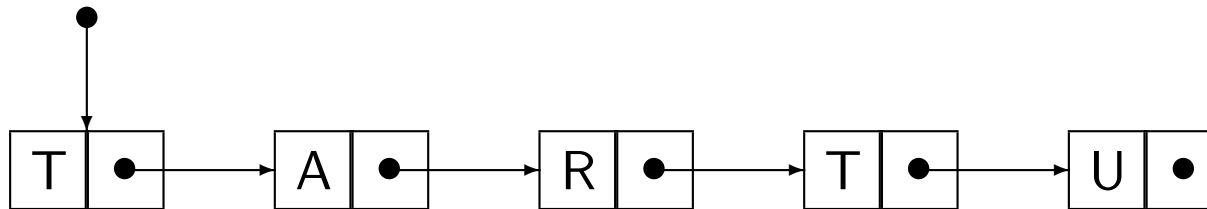
- **Algebraic methods**
- **Vertical modularization**

Equational & inductive reasoning



3.4 Imperative Data Model — *Stacks as Linear Lists*

An **imperative data model** provides **variables** (*storage locations*) and **pointers** (*storage addresses*) to build **state-based implementations** along with **procedures** to manipulate them.



Benefits for systems programming

- **state** *selective updating*
- **pointer** *sharing, manipulation
cyclic structures*
- **storage** *create — destroy*

Object-oriented data model

- **state encapsulation**
- **object identity**
- **life cycle**



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

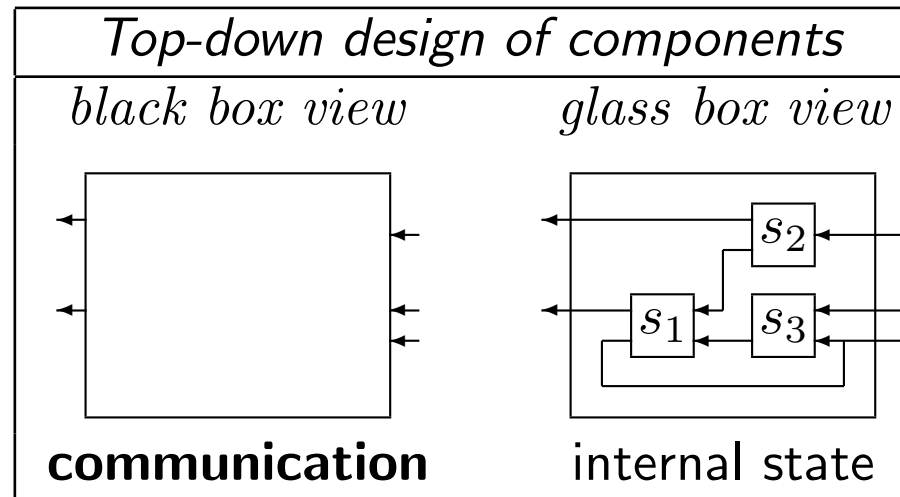
7. Model Transformation

8. Programming Language Models

9. Classification of System Models



4. Interaction Models

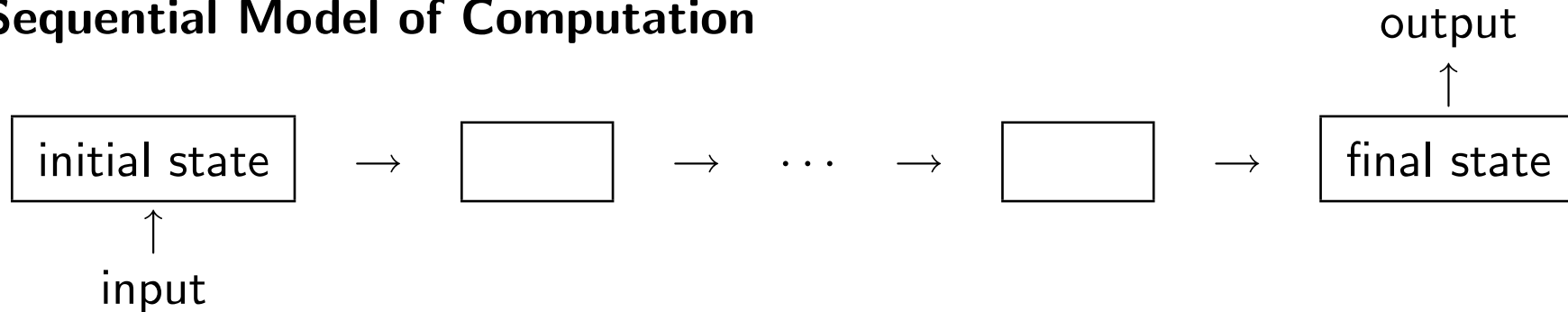


Black box view	Glass box view
<i>Input/output behaviour</i>	<i>Architecture</i>
<i>Service, Composition</i>	<i>Implementation</i>
<i>Correctness, Properties</i>	<i>Efficiency</i>

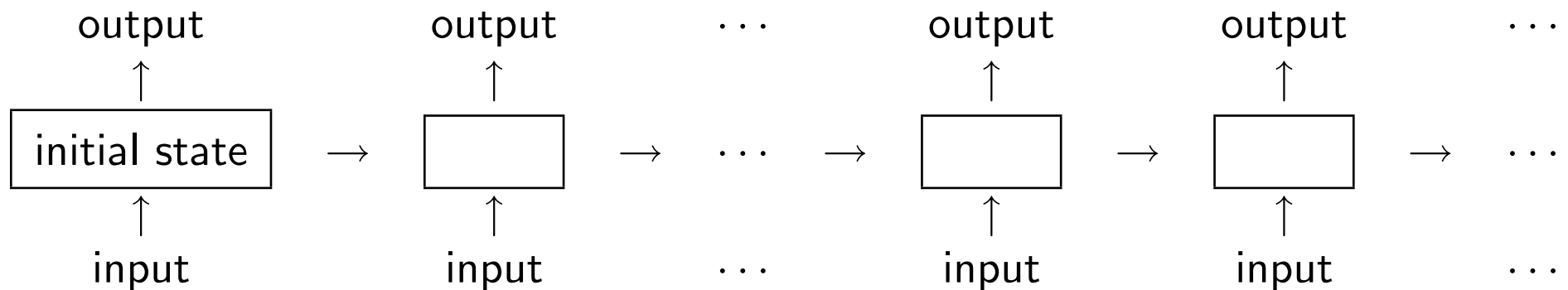


4.1 Models of Computation

Sequential Model of Computation



Interactive Model of Computation



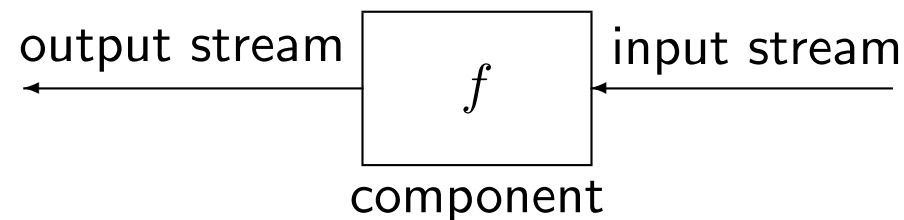
4.2 Streams

Streams model *communication histories on unidirectional channels.*

Finite streams $\mathcal{A}^* = \{\langle x_0, \dots, x_m \rangle \mid x_i \in \mathcal{A}\}$

Concatenation $\langle x_0, \dots, x_m \rangle \ \& \ \langle y_0, \dots, y_n \rangle = \langle x_0, \dots, x_m, y_0, \dots, y_n \rangle$

Prefix relation $X \sqsubseteq Y$ iff $\exists R \in \mathcal{A}^* : X \ \& \ R = Y$
describes *operational progress in time.*



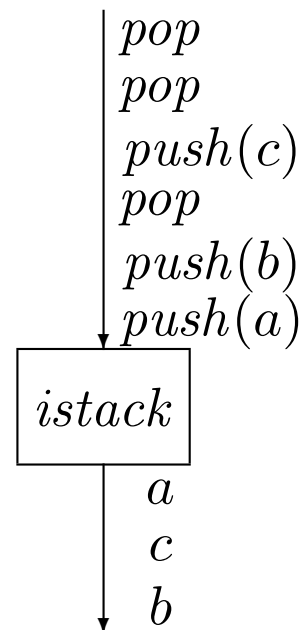
Stream transformer $f : \mathcal{A}^* \rightarrow \mathcal{B}^*$

Monotonicity $X \sqsubseteq Y \Rightarrow f(X) \sqsubseteq f(Y)$

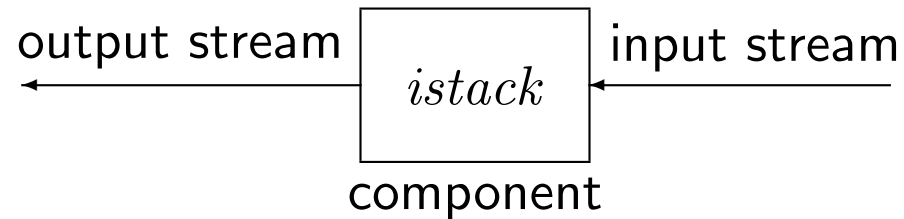


4.3 Interactive Stack — *Informal Description*

An **interactive stack** stores an unbounded number of elements following a *last-in/first-out strategy*. The input consists of *push commands* entering a datum, and *pop commands* requesting the datum stored most recently.



4.4 Interactive Stack — *Regular Behaviour*



Interaction Interface $(\mathcal{I}, \mathcal{O})$

type of input messages: $\mathcal{I} = \{pop, reset\} \cup push(\mathcal{D})$

type of output messages: $\mathcal{O} = \mathcal{D}$

$istack : \mathcal{I}^* \rightarrow \mathcal{O}^*$
--

$istack(Push) = \langle \rangle$

$istack(Push \ \& \ \langle push(d), pop \rangle \ \& \ X) = \langle d \rangle \ \& \ istack(Push \ \& \ X)$
--

$istack(Push \ \& \ \langle reset \rangle \ \& \ X) = istack(X)$
--

$Push \in push(\mathcal{D})^*$



4.5 Interactive Stack — *Irregular Behaviour*

input history									output
<i>push</i> (1)	<i>pop</i>	pop	pop	<i>push</i> (2)	<i>push</i> (3)	<i>push</i> (4)	<i>pop</i>	...	?

fault-sensitive stack

<i>push</i> (1)	<i>pop</i>								⟨1⟩
-----------------	------------	--	--	--	--	--	--	--	-----

fault-tolerant stack

<i>push</i> (1)	<i>pop</i>			<i>push</i> (2)	<i>push</i> (3)	<i>push</i> (4)	<i>pop</i>	...	⟨1, 4...⟩
-----------------	------------	--	--	-----------------	-----------------	-----------------	------------	-----	-----------

robust stack

<i>push</i> (1)	<i>pop</i>	pop	pop	<i>push</i> (2)	<i>push</i> (3)	<i>push</i> (4)	<i>pop</i>	...	⟨1, <i>u</i> , <i>u</i> , 4...⟩
-----------------	------------	------------	------------	-----------------	-----------------	-----------------	------------	-----	---------------------------------

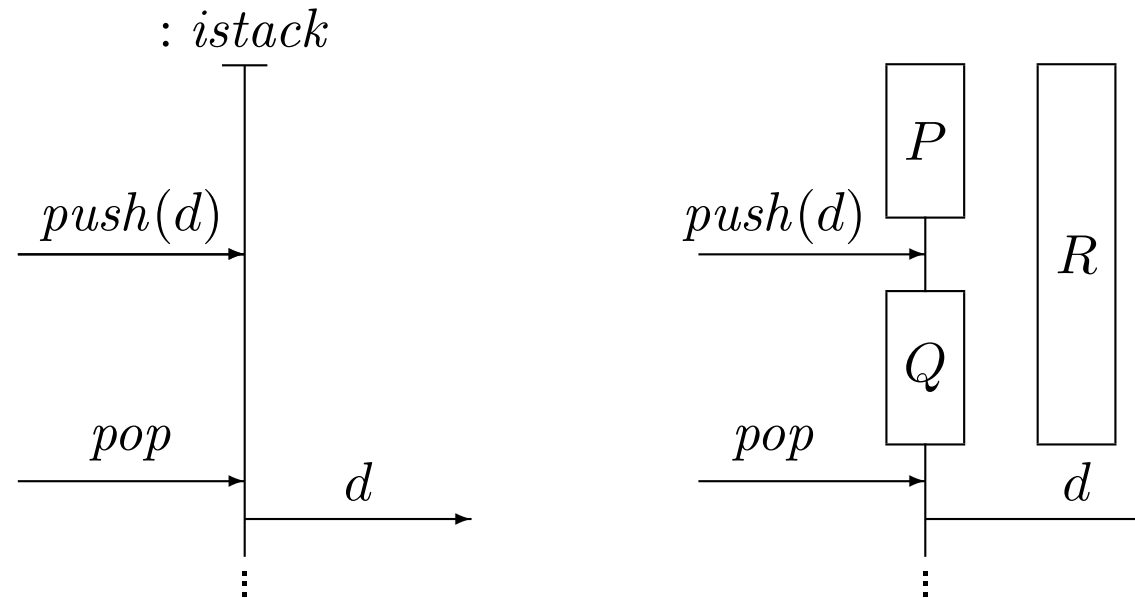
fault-correcting stack

<i>push</i> (1)	<i>pop</i>	pop	pop	<i>push</i> (2)	<i>push</i> (3)	<i>push</i> (4)	<i>pop</i>	...	⟨1, 2, 3, 4...⟩
-----------------	------------	------------	------------	-----------------	-----------------	-----------------	------------	-----	-----------------

A component *guarantees a service* only for input from the **service domain**.



4.6 Interactive Stack — Sequence Diagram (Sample)



$$\begin{aligned}
 & \text{state}(P \ \& \ \langle \text{push}(d) \rangle) &= & \text{state}(P \ \& \ \langle \text{push}(d) \rangle \ \& \ Q) \\
 \wedge & \text{istack}(P \ \& \ \langle \text{push}(d) \rangle \ \& \ Q) &= & R \\
 \Rightarrow & \text{istack}(P \ \& \ \langle \text{push}(d) \rangle \ \& \ Q \ \& \ \langle \text{pop} \rangle) &= & R \ \& \ \langle d \rangle
 \end{aligned}$$

diagram ↔ formalism



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

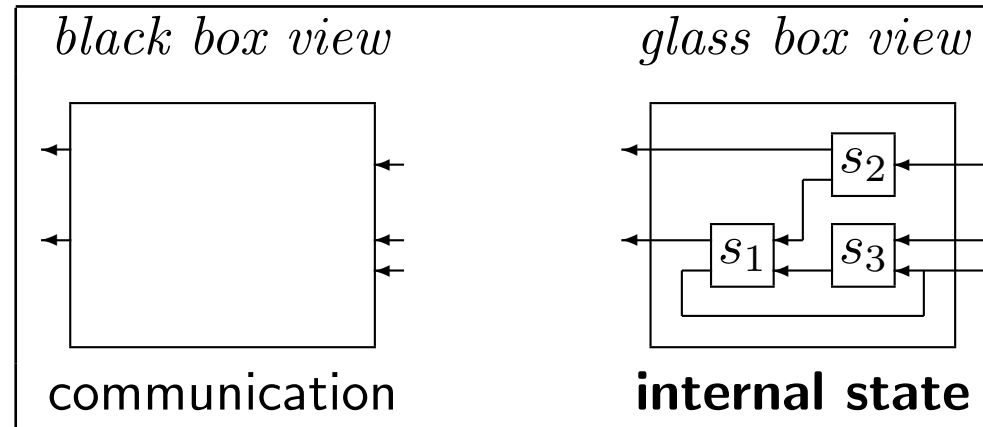
7. Model Transformation

8. Programming Language Models

9. Classification of System Models



5. State-Based Models



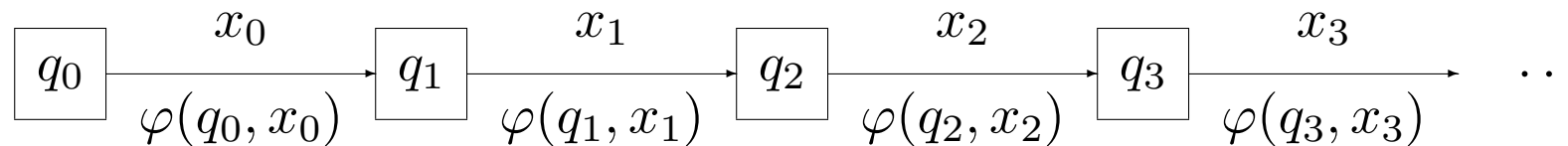
Black box view	Glass box view
<i>Input/output behaviour</i>	<i>Architecture</i>
<i>Service</i>	<i>Implementation</i>
<i>Correctness</i>	<i>Efficiency</i>



5.1 State Transition Machines

Constituents of the machine $M = (Q, \mathcal{I}, \mathcal{O}, \delta, \varphi, q_0)$

set Q of <i>states</i>	one-step <i>state transition function</i>	$\delta : Q \times \mathcal{I} \rightarrow Q$
set \mathcal{I} of <i>input data</i>	one-step <i>output function</i>	$\varphi : Q \times \mathcal{I} \rightarrow \mathcal{O}^*$
set \mathcal{O} of <i>output data</i>	<i>initial state</i>	$q_0 \in Q$



Processing input streams

multi-step <i>state transition function</i>	$\delta^* : Q \rightarrow [\mathcal{I}^* \rightarrow Q]$
multi-step <i>output function</i>	$\varphi^* : Q \rightarrow [\mathcal{I}^* \rightarrow \mathcal{O}^*]$

The multi-step output function $\varphi^*(q)$ is a stream transformer!



5.1 State Transition Machine (cdt.) — *Interactive Stack*

$M = (Q, \mathcal{I}, \mathcal{O}, \delta, \varphi, \langle \rangle)$	
Q	$= \mathcal{D}^* \cup \{fail\}$
$\delta(fail, x)$	$= fail$
$\delta(Q, push(d))$	$= Q \& \langle d \rangle$
$\delta(\langle \rangle, pop)$	$= fail$
$\delta(Q \& \langle d \rangle, pop)$	$= Q$
$\varphi(q, push(d))$	$= \langle \rangle$
$\varphi(fail, pop)$	$= \langle \rangle$
$\varphi(\langle \rangle, pop)$	$= \langle \rangle$
$\varphi(Q \& \langle d \rangle, pop)$	$= \langle d \rangle$

M implements the interactive stack:

$$\varphi^*(\langle \rangle)(X) = istack(X)$$



5.2 State Transition Tables

A **state transition table** displays the *different transition rules* in a clear way:

state	input	state'	output
q	x	$\delta(q, x)$	$\varphi(q, x)$

The **transition rules** relate *current states* and *inputs* to *successor states* (denoted by a prime) and *outputs*.

The *transition rules* **tabulate** the *transition functions* δ and φ for all *possible combinations*.

Interactive Stack

state	input	state'	output
<i>fail</i>	x	<i>fail</i>	$\langle \rangle$
Q	<i>push</i> (d)	$Q \& \langle d \rangle$	$\langle \rangle$
$\langle \rangle$	<i>pop</i>	<i>fail</i>	$\langle \rangle$
$Q \& \langle d \rangle$	<i>pop</i>	Q	$\langle d \rangle$



5.3 State Transition Diagrams

State transition machines can be considered as **labelled directed graphs**:

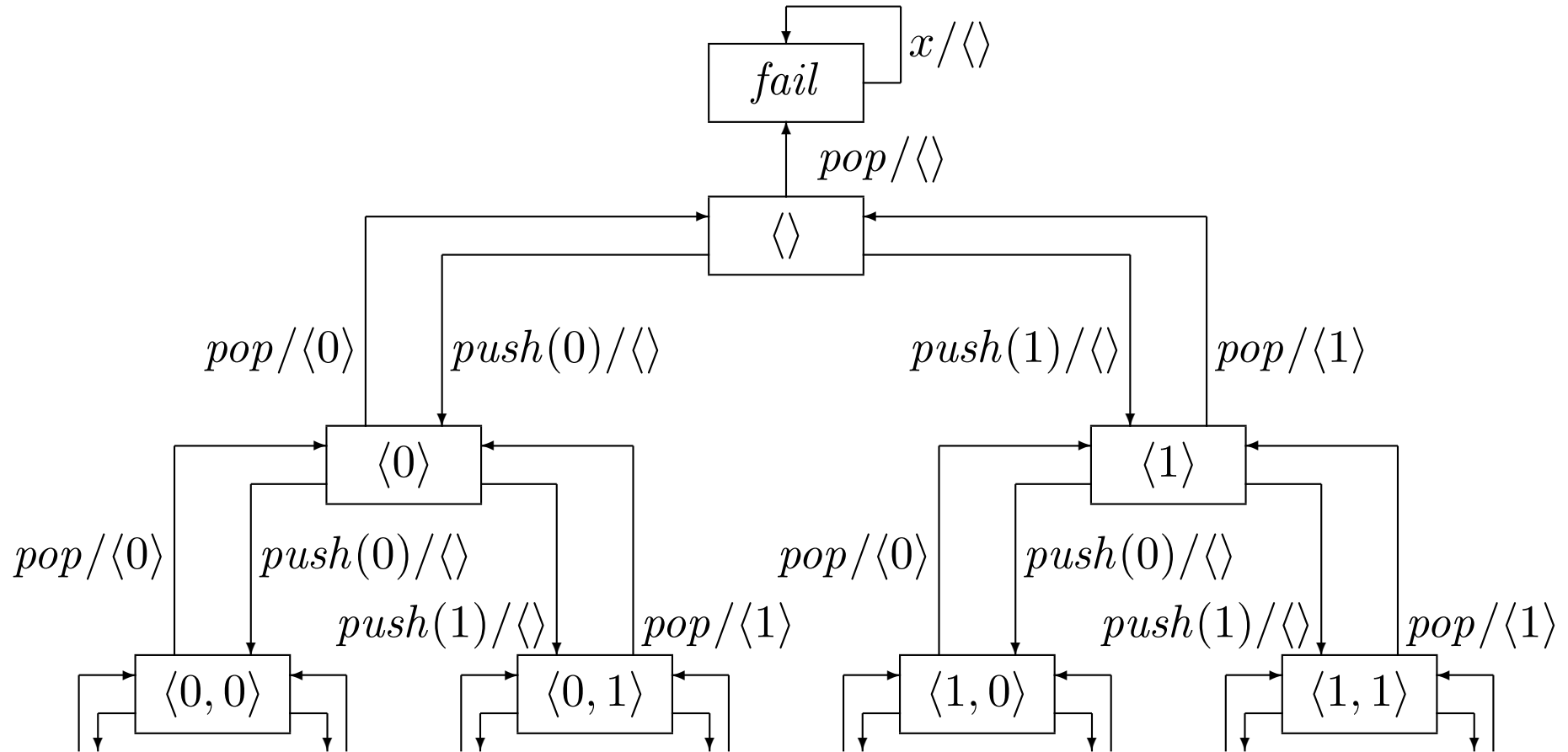
graph		state transition machine
nodes	Q	states
vertices	$q \rightarrow \delta(q, x)$	transitions
labels	$x / \varphi(q, x)$	(input,output)

The finite *symbolic state transition diagram* can be **expanded** into an infinite *state transition diagram* by **instantiating** the four *variables*

$$Q, Q' \in \mathcal{D}^* \quad d \in \mathcal{D} \quad x \in \mathcal{I} .$$

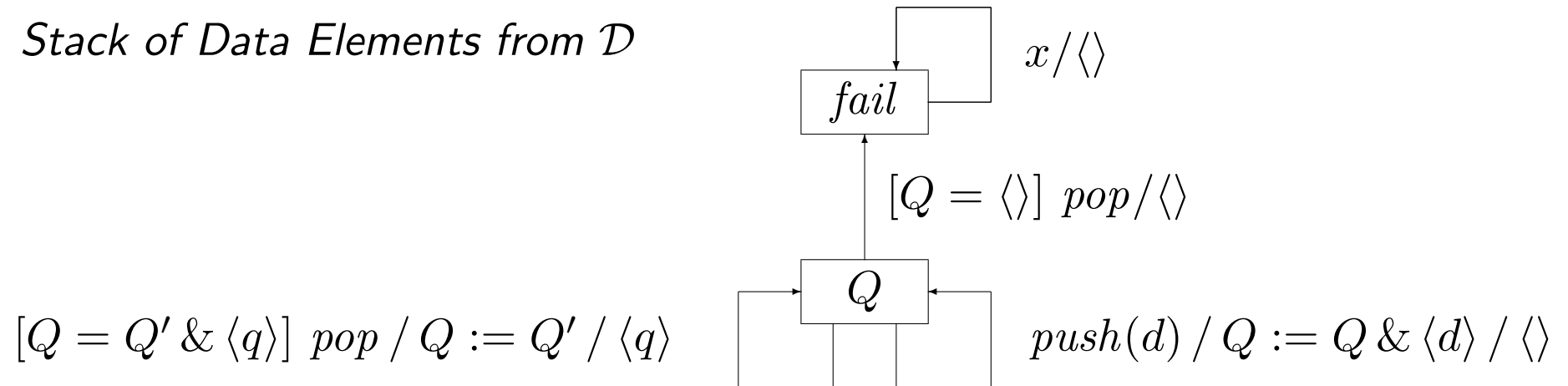


State Transition Diagram (part) for $\mathcal{D} = \{0, 1\}$



5.4 Symbolic State Transition Diagrams

Stack of Data Elements from \mathcal{D}



This **representation** identifies all *regular states* (Q).



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

7. Model Transformation

8. Programming Language Models

9. Classification of System Models



6. Architectural Models

Composite systems are *hierarchically composed of elementary components or subcomponents*.

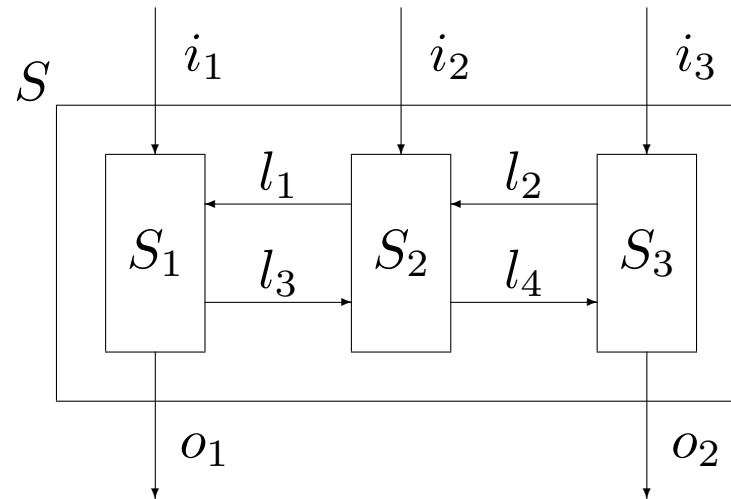
Composite systems can be constructed using a **graphical style** or by **composition operators**.

The **architecture** describes the *static structure of composite systems*.

The **behaviour** of a *composite system* must be inferred from the *behaviours* of its *components*.



6.1 Composition in Graphical Style



$$S : \mathcal{A}_1^\infty \times \mathcal{A}_2^\infty \times \mathcal{A}_3^\infty \rightarrow \mathcal{B}_1^\infty \times \mathcal{B}_2^\infty$$

$$S(i_1, i_2, i_3) = (o_1, o_2)$$

$$S_1(i_1, l_1) = (o_1, l_3)$$

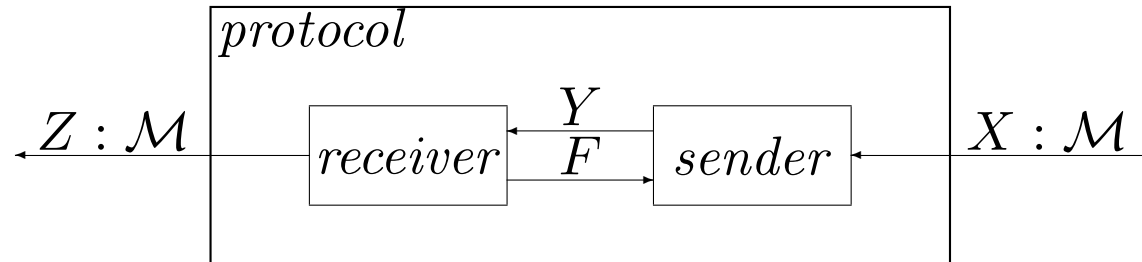
$$S_2(i_2, l_2, l_3) = (l_1, l_4)$$

$$S_3(l_4, i_3) = (l_2, o_2)$$

The composite system is described by a *collection of equations* (net list) using *named input, output and internal channels* based on the descriptions of the subcomponents.



6.2 Protocol Architecture



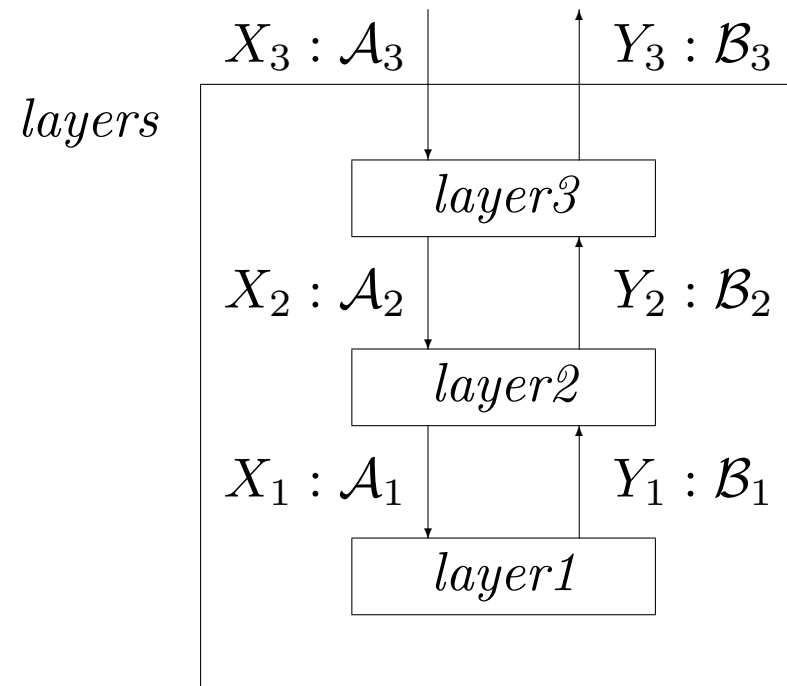
$protocol : \mathcal{M}^* \rightarrow \mathcal{M}^*$	
$protocol(X)$	$= Z$
$sender(F, X)$	$= Y$
$receiver(Y)$	$= (Z, F)$

Correctness

The equation $Z = X$ specifies that no messages are *lost*, *reordered*, *duplicated* or *faked*.



6.3 Layered Architecture



Outline

1. Introduction

2. Modeling

3. Data Models

4. Interaction Models

5. State-Based Models

6. Architectural Models

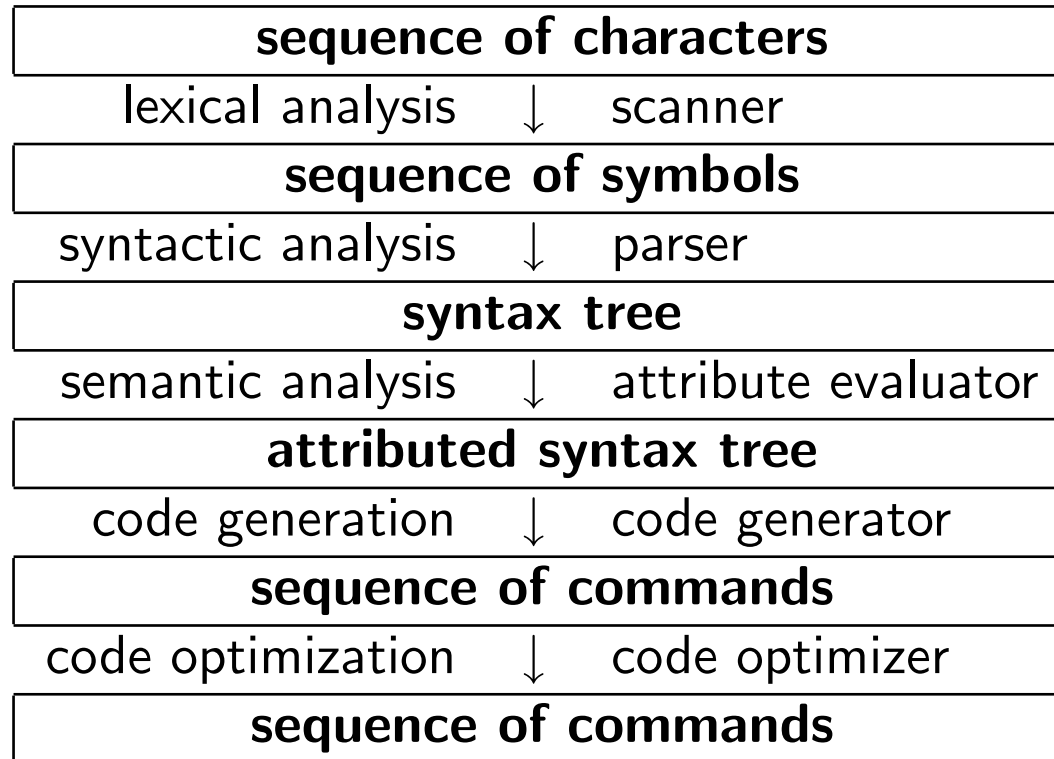
7. Model Transformation

8. Programming Language Models

9. Classification of System Models



7.1 Compilation — From Syntax to Code



7.2 Data Models — From Sig's to Interaction Interfaces

Interaction Interface $(\mathcal{I}, \mathcal{O})$

type of input messages: $\mathcal{I} = \{pop, reset\} \cup push(\mathcal{D})$

type of output messages: $\mathcal{O} = \mathcal{D}$

Transformation *Signature* \mapsto *Interaction Interface*

$$\frac{prefix : data \star stack \rightarrow stack}{push : data \rightarrow [\underline{stack} \rightarrow \underline{stack}]}$$

$$\frac{first : stack \rightarrow data \quad rest : stack \rightarrow stack}{pop : \underline{stack} \rightarrow data \star \underline{stack}}$$

$$\frac{empty : \rightarrow stack}{reset : \underline{stack} \rightarrow \underline{stack}}$$

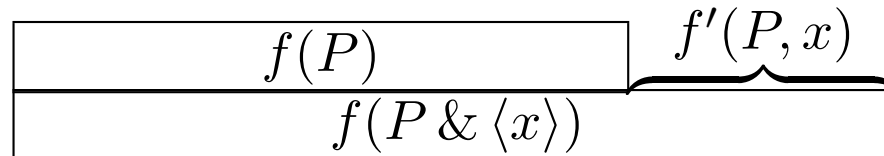
Design Decisions: **Encapsulation** (stack) and **input/output** parameters.



7.3 Data Models — From Streams to States

stream transformer $f : \mathcal{A}^* \rightarrow \mathcal{B}^*$ + *history abstraction* $abstr : \mathcal{A}^* \rightarrow \mathcal{Q}$ → **state transition machine** $M[f, abstr] = (\mathcal{Q}, \mathcal{A}, \mathcal{B}, \delta, \varphi, q_0)$

states	abstractions of input histories	\mathcal{Q}	=	$abstr(\mathcal{A}^*)$
state transition function	extend input history	$\delta(abstr(P), x)$	=	$abstr(P \& \langle x \rangle)$
output function	incremental output	$\varphi(abstr(P), x)$	=	$f'(P, x)$
initial state	empty input history	q_0	=	$abstr(\langle \rangle)$



States are history abstractions.



7.4 Model Refinement

Model refinement is a fundamental notion for *development of systems* from *abstract specifications* to *concrete implementations*.

The *refinement steps* may exploit different **development methods** (*transformation, generation, verification*) for the system under construction.

- **Behavioural Refinement**
- **Interface Refinement**
- **Architectural Refinement**
- **Communication Refinement**
- **State Refinement**
- **Data Refinement**



Outline

1. Introduction
2. Modeling
3. Data Models
4. Interaction Models
5. State-Based Models
6. Architectural Models
7. Model Transformation
- 8. Programming Language Models**
9. Classification of System Models



8.1 Models for Programming Languages — *Disjunction*

The **denotational semantics** provides **models** for *programming language constructs*.

strict disjunction			
<i>or</i>	\perp	T	F
\perp	\perp	\perp	\perp
T	\perp	T	T
F	\perp	T	F

left-right disjunction			
<i>lor</i>	\perp	T	F
\perp	\perp	\perp	\perp
T	T	T	T
F	\perp	T	F

parallel disjunction			
<i>por</i>	\perp	T	F
\perp	\perp	T	\perp
T	T	T	T
\perp	\perp	T	F

Programming languages implement a **three-valued logic**: the result of a Boolean expression is *true*, *false* or *undefined*.



8.2 Models for Schedules — *Fairness and Liveness*

Model the **schedule** for the **nondeterministic unboundedly fair interleaving** of two **infinite processes**.

Generalized regular expression $(0^+ \cdot 1 + 1^+ \cdot 0)^\omega$

Grouping an infinite stream of Boolean values:

$$\langle \underbrace{0, 0, 0, 0, 0, 1}_{\in 0^+ \cdot 1}, \underbrace{1, 1, 1, 0}_{\in 1^+ \cdot 0}, \underbrace{0, 0, 0, 0, 0, 1}_{\in 0^+ \cdot 1}, \underbrace{0, 0, 0, 0, 0, 0, 0, 1}_{\in 0^+ \cdot 1}, \underbrace{1, 1, 1, 1, 0, \dots}_{\in 1^+ \cdot 0} \rangle$$

$(0^+ \cdot 1$	$+$	$1^+ \cdot 0)$	ω
fairness	nondeterministic choice	fairness	
liveness			

Bounded Fairness $(0^{1..m} \cdot 1 + 1^{1..m} \cdot 0)^\omega$ $(m \geq 1)$



Outline

1. Introduction
2. Modeling
3. Data Models
4. Interaction Models
5. State-Based Models
6. Architectural Models
7. Model Transformation
8. Programming Language Models
- 9. Classification of System Models**



9. Classification of System Models

layout	<i>static</i> topological	dynamic metric
communication	synchronous <i>unidirectional</i>	<i>asynchronous</i> bidirectional
state	<i>state-full</i> continuous <i>simple</i> shared	<i>state-less</i> <i>discrete</i> <i>structured</i> <i>distributed</i>
time	timed continuous sensitive	<i>untimed</i> discrete invariant
control	<i>(non)deterministic</i> centralized event-driven	stochastic <i>distributed</i> time-driven



programming = modeling on code level

What are **unifying higher-level models** for
software and system engineering

to cope with

⋮

architectures, components

interfaces, services

⋮

on different

levels of abstraction

integrating different

system views?

Acknowledgements ISP team, in particular A. STÜMPEL and B. DÖLLE

